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## SPACE RADIATION TRANSPORT RESULTS

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# INTRODUCTION: SI UNITS

m  $\equiv$  meter, s  $\equiv$  second, kg  $\equiv$  kilogram, N  $\equiv$  Newton, J  $\equiv$  Joule

- Distance  $x$  [m], Time  $t$  [s]
- Speed (velocity)  $v \equiv \frac{dx}{dt}$  or  $v \equiv \frac{\Delta x}{\Delta t}$   
 $v$  [m per s  $\equiv$  m/s  $\equiv$  m s $^{-1}$ ]
- Acceleration  $a \equiv \frac{dv}{dt} = \frac{d^2x}{dt^2}$  or  $a \equiv \frac{\Delta v}{\Delta t}$   
 $a$  [m/s $^2 \equiv$  m s $^{-2}$ ]
- Force  $F = ma$   
 $m$  [kg],  $F$  [N  $\equiv$  kg m s $^{-2}$ ]
- Work  $W \equiv \int F dx$  or  $W \equiv F \Delta x$   
 $W$  [J  $\equiv$  N m]
- Energy  $W \equiv \Delta E = \int F dx$  (Kinetic Energy, Potential Energy, Mass Energy)  
 $E$  [J] or [eV] [eV  $\equiv 1.602 \times 10^{-19}$  J]

# INTRODUCTION: AREAL DENSITY

- Ordinary thickness doesn't tell you amount of material traversed
  - $d = 20$  cm Water vs.  $d = 20$  cm Aluminum
  - more material traversed in Al, even though distance  $d$  same
- Areal density  $x = d\rho$ 
  - $x$  [g/cm<sup>2</sup>]
  - $d$  [cm]
  - $\rho$  [g/cm<sup>3</sup>]
- $x = 20$  g/cm<sup>2</sup>
  - $\rho_{\text{water}} = 1$  g/cm<sup>3</sup>       $\rho_{\text{Al}} = 2.7$  g/cm<sup>3</sup>
  - $d_{\text{water}} = 20$  cm       $d_{\text{Al}} = 7.4$  cm
- Same amount of material traversed in 20 cm Water and 7.4 cm Al
- $x_{\text{ISS}} \approx 15$  g/cm<sup>2</sup>,  $x_{\text{Mars Atmosph}} \approx 20$  g/cm<sup>2</sup>,  $x_{\text{Earth Atmosph}} \approx 1000$  g/cm<sup>2</sup>

# INTRODUCTION: RELATIVITY

- $E = mc^2$
- $E \equiv T + m_0c^2$ 
  - $E \equiv$  Total energy
  - $T \equiv$  Kinetic energy, often written  $E$  !!!!!!!!!
  - $m_0 \equiv$  Rest mass energy
  - $m \equiv \gamma m_0$  ,  $\Rightarrow E = \gamma m_0 c^2$
  - $\gamma \equiv \frac{1}{\sqrt{1-(v/c)^2}}$  ,  $\beta \equiv v/c \Rightarrow \gamma = \frac{1}{\sqrt{1-\beta^2}}$
- Note:  $T = E - m_0c^2 \neq \frac{1}{2}mv^2$   
 $\approx \frac{1}{2}mv^2$  if  $v \ll c$

# INTRODUCTION: MeV / NUCLEON

KINETIC ENERGY: PEOPLE WRITE E, BUT THEY MEAN T !!!

- $E = T + m_0c^2 = mc^2 = \gamma m_0c^2$

Calculate speed

$$\frac{1}{\sqrt{1-(v/c)^2}} \equiv \gamma = \frac{T}{m_0c^2} + 1$$

$$\hat{T} \text{ [MeV/n]} \Rightarrow T = A\hat{T}$$

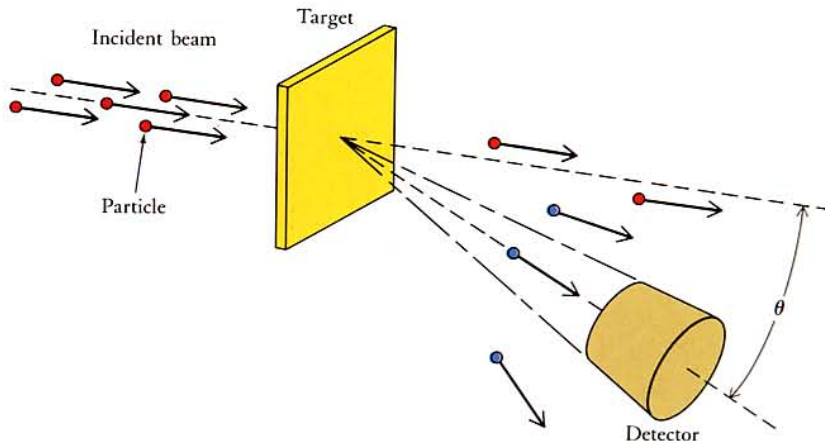
$$m_0 = Am_n, \quad m_n \equiv m_{\text{nucleon}} = 938 \text{ MeV}/c^2$$

$$\gamma = \frac{T}{m_0c^2} + 1 = \frac{A\hat{T}}{Am_nc^2} + 1 = \frac{\hat{T}}{m_nc^2} + 1$$

E.g. What is speed of 1000 MeV/n  $^{56}\text{Fe}$  projectile?

# CROSS SECTION

- Typical scattering experiment: beam of particles fired into a target
- Surrounding detectors detect the particles coming out of reaction



[Lederman & Schramm, From quarks to the cosmos, Freeman, New York, 1989]

# CROSS SECTION

- Let's say that some protons are detected
- If one just counts the total number  $N$  of protons emitted *per unit time* then this is related to the total cross section by

$$N \equiv \mathcal{L} \sigma$$

- $\mathcal{L}$  = luminosity of beam
- $\sigma$  = cross section - related to *probability* that reaction will occur (that a proton will be emitted)
- Above formula: more particles will be detected if reaction probability is large **or** if we have very intense beam



# CROSS SECTION

- Luminosity typically measured in  $\text{cm}^{-2} \text{s}^{-1}$
- E.g. Fermilab proton beam (2000) was about  $\mathcal{L} = 10^{32} \text{ cm}^{-2} \text{s}^{-1}$
- Cross section is measured in units of area namely  $\text{cm}^2$
- $N = \mathcal{L}\sigma$  gives units of *counts per second*
- Note that

$$\text{barn} = 10^{-28} \text{ m}^2 = 10^{-24} \text{ cm}^2$$

and a *picobarn* (pb) is therefore (pico  $\equiv 10^{-12}$ )

$$\text{pb} = 10^{-36} \text{ cm}^2$$

- Fermilab luminosity can be re-written

$$\mathcal{L} = 10^{32} \text{ cm}^{-2} \text{s}^{-1} = 10^{-4} \text{ pb}^{-1} \text{s}^{-1}$$

# CROSS SECTION

- Sometimes accelerator administrators use integrated luminosity  $\mathcal{L}_{\text{int}}$ , which is simply luminosity multiplied by time

$$\mathcal{L}_{\text{int}} = \mathcal{L} t$$

- E.g. if Fermilab ran continuously over a year, this would correspond to an integrated luminosity of

$$\mathcal{L}_{\text{int}}^{\text{1year}} = 10^{-4} \text{pb}^{-1} \text{s}^{-1} \times 365 \text{ days} \approx 3000 \text{pb}^{-1}$$

- If the accelerator only delivered say  $1500 \text{pb}^{-1}$  then that would mean it was shut down for half the time
- Integrated luminosity related to integrated number of counts  $N_{\text{int}}$  (total number of counts, *not* number of counts per unit time) by

$$N_{\text{int}} = N t$$

where  $N$  is number of counts per unit time from before  $N = \mathcal{L} \sigma$

# CROSS SECTION

- Ice puck collisions:
  - Kinetic energy conserved if surface frictionless
- Particle collisions
  - Often kinetic energy *not* conserved
  - Especially if new particles are created, e.g.  $p+p \rightarrow p+p+\pi^0$
  - Or particles are lost (absorbed), e.g.  $p + {}^{12}\text{C} \rightarrow {}^{13}\text{N}$
- Total energy  $E$  **always** conserved (just like momentum & charge)
- **Elastic collision  $\equiv$  Kinetic energy conserved**
  - Does *not* mean that incident KE remains same
  - E.g. **Neutron can undergo elastic collision  $\Rightarrow$  impart KE to proton**
- **Inelastic collision  $\equiv$  Kinetic energy *not* conserved**

# CROSS SECTION

- **Total** cross section

- second definition of the word “total”

$$\sigma_{\text{total}} \equiv \sigma_{\text{elastic}} + \sigma_{\text{inelastic}} + \sigma_{\text{absorption}}$$

- **Scattering** cross section is defined as

$$\sigma_{\text{scattering}} \equiv \sigma_{\text{elastic}} + \sigma_{\text{inelastic}}$$

$$\Rightarrow \sigma_{\text{total}} \equiv \sigma_{\text{scattering}} + \sigma_{\text{absorption}}$$

- **Reaction** cross section is defined as

$$\sigma_{\text{reaction}} \equiv \sigma_{\text{inelastic}} + \sigma_{\text{absorption}}$$

$$\Rightarrow \sigma_{\text{total}} \equiv \sigma_{\text{elastic}} + \sigma_{\text{reaction}}$$

- Some authors write (including me!)

$$\sigma_{\text{total}} \equiv \sigma_{\text{elastic}} + \sigma_{\text{inelastic}}$$

where  $\sigma_{\text{reaction}} \equiv \sigma_{\text{inelastic}}$

# CROSS SECTION

## EXAMPLE: NEUTRON INTERACTIONS WITH NUCLEI

[Lamarsh, Nuclear reactor theory, Addison-Wesley, Reading, Massachusetts, 1966]

- **Elastic** scattering  $\Rightarrow$  Kinetic Energy (KE) conserved
  - Nucleus unchanged in isotopic composition or internal energy
  - KE of neutron and nucleus can change (but total KE conserved)
  - Neutron can transfer KE to nucleus
  - Neutron reappears after interaction (n,n)
- **Inelastic** scattering  $\Rightarrow$  KE not conserved
  - Nucleus left in excited state
  - Neutron reappears after interaction (n,n')
- Neutron scattered elastically (n,n) or inelastically (n,n')
  - Neutron reappears after interaction
- **Absorption** reaction  $\Rightarrow$  Neutron disappears
  - Examples (n, $\gamma$ ), (n,p), (n, $\alpha$ ), fission (by convention)

*Notation:* (a,b) means  $a + \text{target} \rightarrow b + \text{anything}$

# CROSS SECTION

## EXAMPLE: NEUTRON INTERACTIONS WITH NUCLEI

[Lamarsh, Nuclear reactor theory, Addison-Wesley, Reading, Massachusetts, 1966]

- Definitions differ from previous slides, but Lamarsh definitions clearer

$$\sigma_{\text{total}} \equiv \sigma_{\text{elastic}(n,n)} + \sigma_{\text{inelastic}(n,n')} + \sigma_{(n,\gamma)} + \sigma_{(n,p)} + \sigma_{(n,2n)} + \sigma_{(n,3n)} \\ + \sigma_{(n,pn)} + \sigma_{(n,\alpha)} + \sigma_{(n,\text{fission})} + \dots$$

$$\sigma_{\text{total}} \equiv \sigma_{\text{elastic}} + \sigma_{\text{nonelastic}}$$

$$\sigma_{\text{nonelastic}} = \sigma_{\text{inelastic}} + \sigma_{(n,\gamma)} + \sigma_{(n,p)} + \sigma_{(n,2n)} + \sigma_{(n,3n)} \\ + \sigma_{(n,pn)} + \sigma_{(n,\alpha)} + \sigma_{(n,\text{fission})} + \dots$$

$$\sigma_{\text{absorption}} = \sigma_{(n,\gamma)} + \sigma_{(n,p)} + \sigma_{(n,\alpha)} + \sigma_{(n,\text{fission})} + \dots$$

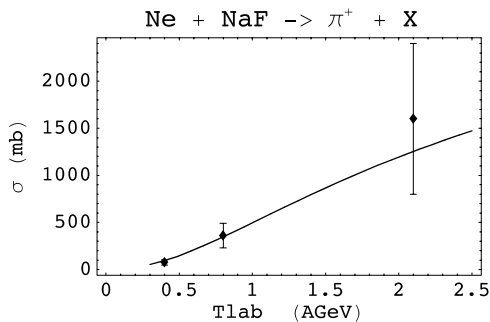
$$\sigma_{\text{nonelastic}} = \sigma_{\text{inelastic}} + \sigma_{\text{absorption}} + \sigma_{(n,2n)} + \sigma_{(n,3n)} + \sigma_{(n,pn)} + \dots$$

*Note:*  $\sigma_{\text{nonelastic}} \neq \sigma_{\text{inelastic}}$

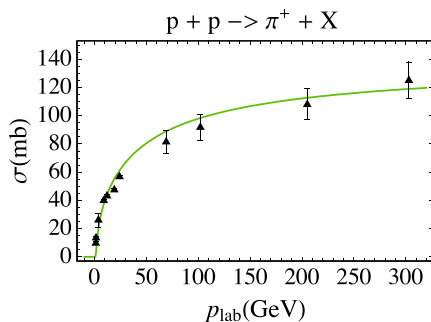
# TOTAL CROSS SECTION

Projectile + Target  $\rightarrow$  Detected particles

- Count total number of detected particles
  - Total cross section  $\sigma$
  - Easiest to measure, hardest to calculate (from QFT)



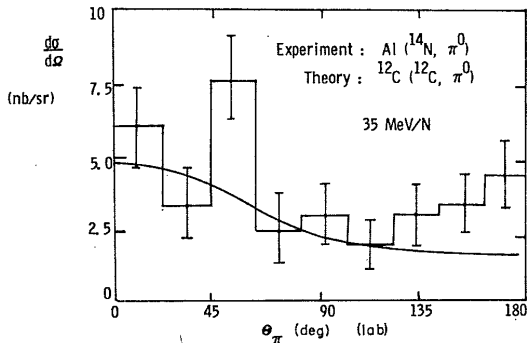
[Norbury, Nucl. Inst. Meth. B 254, 187, 2007],



[Norbury, Nucl. Inst. Meth. B 267, 1209, 2009]

# SINGLE DIFFERENTIAL CROSS SECTION

- Count particles at different angles (e.g.  $\theta = 0^\circ, 30^\circ, 60^\circ, 90^\circ$ )
  - Angular **differential** cross section  $\frac{d\sigma}{d\theta} \equiv \sigma(\theta)$  (Angular distribution)
  - $\sigma = \int_0^{2\pi} \frac{d\sigma}{d\theta} d\theta = \int_0^{2\pi} \sigma(\theta) d\theta$   $d\Omega = 2\pi \sin \theta d\theta$
  - **Harder to measure**

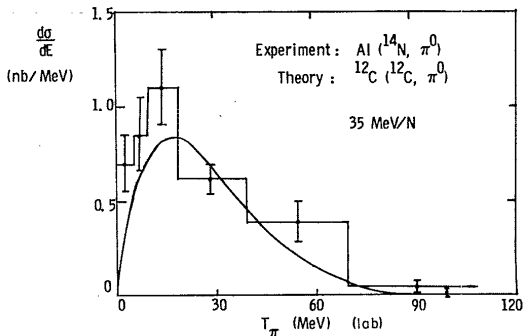


[Norbury, Physical Review C 37, 407,1988]



# SINGLE DIFFERENTIAL CROSS SECTION

- Count particles of different energies (e.g.  $E = 5$  MeV, 10 MeV, 20 MeV)
  - Energy **differential** cross section  $\frac{d\sigma}{dE} \equiv \sigma(E)$  (Spectral distribution)
  - Energy =  $E \equiv$  Kinetic Energy!!
  - $\sigma = \int_0^{E_{\max}} \frac{d\sigma}{dE} dE = \int_0^{E_{\max}} \sigma(E) dE$



[Norbury, Physical Review C 37, 407,1988]

# DOUBLE DIFFERENTIAL CROSS SECTION

- Count particles of different energies and at different angles

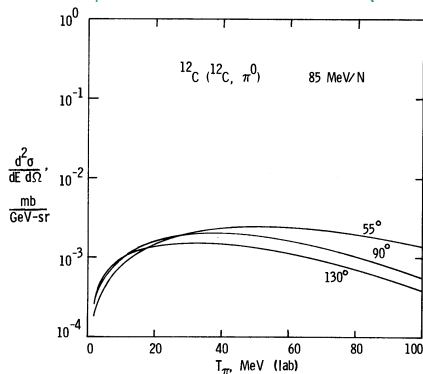
e.g. ( $\theta = 30^\circ$  for  $E = 5$  MeV, 10 MeV) and ( $\theta = 60^\circ$  for  $E = 5$  MeV, 10 MeV)

- Double differential cross section  $\frac{d^2\sigma}{dE d\theta} \equiv \sigma(E, \theta)$

- $\sigma = \int \frac{d^2\sigma}{dE d\theta} dE d\theta = \int \sigma(E, \theta) dE d\theta$

- $\frac{d\sigma}{d\theta} = \int \frac{d^2\sigma}{dE d\theta} dE = \int \sigma(E, \theta) dE, \quad - \frac{d\sigma}{dE} = \int \frac{d^2\sigma}{dE d\theta} d\theta = \int \sigma(E, \theta) d\theta$

- Hardest to measure, Easiest to calculate (from QFT)



[Norbury et al., NASA Technical Paper 2600, 1986]

# TOTAL CROSS SECTION - TWO USES OF WORD “TOTAL”

- **Total  $\equiv$  Elastic + Inelastic** (or Total  $\equiv$  Elastic + Inelastic + Absorption)

Example:  $\sigma_{\text{total}} \equiv \sigma_{\text{elastic}} + \sigma_{\text{inelastic}}$

Example:  $\frac{d\sigma_{\text{total}}}{d\theta} \equiv \frac{d\sigma_{\text{elastic}}}{d\theta} + \frac{d\sigma_{\text{inelastic}}}{d\theta}$

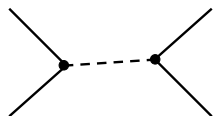
- **Total  $\equiv$  Non-differential**

$$\sigma \equiv \int \frac{d\sigma}{d\theta} d\theta = \int \frac{d\sigma}{dE} dE = \int \frac{d^2\sigma}{dEd\theta} dEd\theta = \int \sigma(E, \theta) dEd\theta$$

Example:  $\sigma_{\text{inelastic}} = \int \frac{d\sigma_{\text{inelastic}}}{d\theta} d\theta$

- $\sigma$  “total - total”  $\sigma_{\text{total}} = \int \frac{d\sigma_{\text{total}}}{d\theta} d\theta = \int \frac{d\sigma_{\text{elastic}}}{d\theta} d\theta + \int \frac{d\sigma_{\text{inelastic}}}{d\theta} d\theta$

## RECAP: DOUBLE DIFFERENTIAL CROSS SECTION



$$\Rightarrow \sigma(E, \theta) \equiv \frac{d^2\sigma}{dE d\theta}$$
$$\equiv \sigma(E, E', \theta, \theta') \text{ later in BTE}$$

- Often called 3-dimensional (3d)
- Very precise information
- Function of both energy & angle
- Ultimate test of nuclear theory
- Needed for 3d transport

## RECAP: SINGLE DIFFERENTIAL CROSS SECTION

$$\sigma(E) = \int d\theta \sigma(E, \theta)$$

$\equiv \sigma(E, E')$  later in BTE

$$\frac{d\sigma}{dE} = \int d\theta \frac{d^2\sigma}{dEd\theta}$$

$$\sigma(\theta) = \int dE \sigma(E, \theta)$$

$$\frac{d\sigma}{d\theta} = \int dE \frac{d^2\sigma}{dEd\theta}$$

- Less precise information
- Function of energy OR angle

## RECAP: TOTAL ( $\equiv$ NON-DIFFERENTIAL) CROSS SECTION

$$\sigma = \int dE \sigma(E) = \int d\theta \sigma(\theta) = \int dE d\theta \sigma(E, \theta)$$

$\equiv \sigma(E)$  later in BTE

- Very crude
- No angle or energy dependence
- Just total number of counts

# CROSS SECTION: EXCLUSIVE VS. INCLUSIVE

EXCLUSIVE:  $A + B \rightarrow C + D + E + F$

- Ultimate theoretical test
- Hard to measure

INCLUSIVE:  $A + B \rightarrow C + \textit{anything}$

- Very crude theoretical test
- Easy to measure

# BETHE - BLOCH EQUATION

[RMP1260, NCRP153-62, Jackson628, Alpen369, NASARP1257-34,40,73, RPP]

## BETHE - BLOCH EQUATION

$\hbar\omega$  = MEAN EXCITATION ENERGY

$$\frac{dE}{dx} = 4\pi N_T Z_T \frac{Z_P^2 e^4}{mc^2 \beta^2} \left[ \ln \left( \frac{2\gamma^2 \beta^2 mc^2}{\hbar\omega} \right) - \beta^2 + \text{corrections} \right]$$



# BOLTZMANN TRANSPORT EQUATION

## 1-DIMENSIONAL TRANSPORT EQUATION

$$\left[ \frac{\partial}{\partial x} - \frac{\partial}{\partial E} S_i(E) + \tilde{\sigma}_i(E) \right] \phi_i(x, E) = \sum_j \int_E^\infty dE' \tilde{\sigma}_{ij}(E, E') \phi_j(x, E')$$

Solve for

$\phi_i(x, E)$  = differential fluence of **isotope**  $i$  at position  $x$  with energy  $E$

$\tilde{\sigma}_i(E) \equiv \tilde{\sigma}_{\text{total}} =$  **isotopic** total cross sect. for **isotope**  $i$  with energy  $E$

$\sigma_{\text{total}} = \sigma_{\text{elastic}} + \sigma_{\text{nonelastic}} = \sigma_{\text{elastic}} + \sigma_{\text{inelastic}} + \sigma_{\text{absorption}} + \sigma_{\text{other}}$

$\tilde{\sigma}_{ij}(E, E')$  = inclusive **isotopic** energy (single) differential cross section for producing **isotope**  $i$  with energy  $E$  from **isotope**  $j$  with energy  $E'$

Different materials:  $\tilde{\sigma}$  are cross sections for specific target material

Note:  $\frac{\partial}{\partial E} S_i(E) \phi_i(x, E) \equiv \frac{\partial}{\partial E} [S_i(E) \phi_i(x, E)]$

# BOLTZMANN TRANSPORT EQUATION - UNITS

## 1-DIMENSIONAL TRANSPORT EQUATION

$$\left[ \frac{\partial}{\partial x} - \frac{\partial}{\partial E} S_i(E) + \tilde{\sigma}_i(E) \right] \phi_i(x, E) = \sum_j \int_E^\infty dE' \tilde{\sigma}_{ij}(E, E') \phi_j(x, E')$$

- $\phi \sim [\text{anything}]$ ,  $x \sim [\text{g/cm}^2] \Rightarrow \tilde{\sigma}_i(E) \sim [\text{cm}^2/\text{g}]$
- 12 g of  $^{12}\text{C}$  contains  $N_A$  molecules, where  $N_A = 6.02 \times 10^{23}$   
 $^{12}\text{C}$ : number density  $\equiv$  number per gram  $= \tilde{\rho} [\text{\#}/\text{g}] = N_A/12 [\text{g}^{-1}]$   
In general,  $\tilde{\rho} [\text{\#}/\text{g}] \equiv N_A/A [\text{g}^{-1}]$
- $\tilde{\rho} = \frac{n}{\rho}$ ,  $n = \# \text{ atoms}/\text{cm}^3$  (number density),  $\rho = \text{"normal" mass density} [\text{g}/\text{cm}^3]$
- Thus,  $\tilde{\sigma} = \tilde{\rho} \sigma \sim [\text{cm}^2/\text{g}] = [\text{g}^{-1} \text{cm}^2]$
- $S_i(E) = \frac{dE}{dx} \Rightarrow \frac{\partial}{\partial E} S_i(E) = \frac{\partial}{\partial E} \frac{dE}{dx}$  same units as  $\frac{\partial}{\partial x}$ . Note:  $L = \frac{dE}{dx} [\frac{\text{MeV}}{\text{cm}}]$ , but  $\frac{L}{\rho} [\frac{\text{MeV}}{\text{g}/\text{cm}^2}]$
- $\tilde{\sigma}_{ij}(E, E') \equiv \frac{d\tilde{\sigma}_{ij}(E')}{dE} \sim [\text{g}^{-1} \text{cm}^2 \text{E}^{-1}]$
- Let differential fluence  $\phi_i(x, E) \sim [\# \text{cm}^{-2} \text{E}^{-1}]$
- $E \sim [\text{anything}]$ , because cancel everywhere, Typically  $E \sim [\text{A MeV}]$

# BOLTZMANN TRANSPORT EQUATION

## 3-DIMENSIONAL TRANSPORT EQUATION

$$\left[ \boldsymbol{\Omega} \cdot \boldsymbol{\nabla} - \frac{\partial}{\partial E} S_i(E) + \tilde{\sigma}_i(E) \right] \phi_i(\mathbf{r}, \boldsymbol{\Omega}, E) = \sum_j \int dE' d\boldsymbol{\Omega}' \tilde{\sigma}_{ij}(\boldsymbol{\Omega}, \boldsymbol{\Omega}', E, E') \phi_j(\mathbf{r}, \boldsymbol{\Omega}', E')$$

Solve for  $\phi_i(\mathbf{r}, \boldsymbol{\Omega}, E)$  = differential fluence of **isotope**  $i$  at  $\mathbf{r}$  moving in direction  $\boldsymbol{\Omega}$  with energy  $E$

$\tilde{\sigma}_i(E)$  = **isotopic** total absorption cross sect. of **isotope**  $i$  with energy  $E$   
 $\equiv \sigma$  before

$\tilde{\sigma}_{ij}(\boldsymbol{\Omega}, \boldsymbol{\Omega}', E, E')$  = inclusive **isotopic** double differential cross section for producing **isotope**  $i$  moving in direction  $\boldsymbol{\Omega}$  with energy  $E$  from **isotope**  $j$  moving in direction  $\boldsymbol{\Omega}'$  with energy  $E'$

$\equiv \sigma(\boldsymbol{\Omega}, E)$  before

# DOSE

- Absorbed dose [ICRU93]  $D \equiv \frac{d\epsilon}{dm}$ 
  - Units [  $\text{Gy} \equiv \text{J kg}^{-1}$  ]
  - $d\epsilon$  = mean energy deposited in mass  $dm$
- Dose deposited at position  $x$  obtained by  $\sum$  over all particles  $j$

## DOSE CALCULATED WITH DIFFERENTIAL FLUENCE $\phi$

$$D(x) = \sum_j \int_0^\infty dE S_j(E) \phi_j(x, E) \quad [\text{Gy} \equiv \text{J kg}^{-1}]$$

- $S_j(E)$  = stopping power as function of particle kinetic energy  $E$
- $\phi_j(x, E)$  = differential particle fluence at position  $x$
- $dE S_j(E) \phi_j(x, E) \sim [\text{MeV}] \left[ \frac{\text{MeV}}{\text{g/cm}^2} \right] \left[ \frac{\#}{\text{cm}^2 \text{MeV}} \right] \sim \left[ \frac{\text{MeV}}{\text{g}} \right]$

# DOSE

- $\phi_j(x, E)$  = differential particle fluence at position  $x$   $\left[ \frac{\#}{\text{cm}^2 \text{MeV}} \right]$
- $\Phi_j$  = particle fluence (integrated)  $\left[ \frac{\#}{\text{cm}^2} \right]$  (Borak, Nelson lectures)  
good for a beam of fixed  $Z$ , fixed  $E$ , then LET fixed

## DOSE CALCULATED WITH INTEGRAL FLUENCE $\Phi$

If  $L$  has units  $\left[ \frac{\text{MeV}}{\text{g/cm}^2} \right]$ :

$$D = L \Phi \quad \left[ \frac{\text{MeV}}{\text{g/cm}^2} \right] \left[ \frac{\#}{\text{cm}^2} \right] = \left[ \frac{\text{MeV}}{\text{g}} \right] \sim \left[ \frac{\text{J}}{\text{kg}} \right]$$

If  $L$  has units  $\left[ \frac{\text{MeV}}{\text{cm}} \right]$ :

$$D = \frac{L}{\rho} \Phi \quad \left[ \frac{\text{MeV/cm}}{\text{g/cm}^3} \right] \left[ \frac{\#}{\text{cm}^2} \right] = \left[ \frac{\text{MeV}}{\text{g}} \right] \sim \left[ \frac{\text{J}}{\text{kg}} \right] \quad (\text{Borak, Nelson})$$

# DOSE - UNIT CONVERSION FACTOR

Assume  $L$  has units  $[\frac{\text{keV}}{\mu\text{m}}]$  (Borak, Nelson)

$$\begin{aligned} D &= \frac{L}{\rho} \Phi \\ &\sim \frac{\text{keV}/\mu\text{m}}{\text{g}/\text{cm}^3} \text{cm}^{-2} = \frac{\text{keV}}{\text{g}} \frac{\text{cm}}{\mu\text{m}} \\ &= \frac{10^3 \text{eV}}{10^{-3} \text{kg}} \frac{10^{-2} \text{m}}{10^{-6} \text{m}} = 10^{10} \frac{\text{eV}}{\text{kg}} = 10^{10} \frac{1.602 \times 10^{-19} \text{J}}{\text{kg}} \\ &= 1.602 \times 10^{-9} \frac{\text{J}}{\text{kg}} \\ &= 1.602 \times 10^{-9} \text{Gy} = 1.602 \times 10^{-7} \text{cGy} \end{aligned}$$

## DOSE CONVERSION FACTOR

$$D = \frac{L}{\rho} \Phi = 1.602 \times 10^{-9} \text{Gy} \quad \text{with } L \sim [\frac{\text{keV}}{\mu\text{m}}], \Phi \sim [\text{cm}^{-2}], \rho \sim [\frac{\text{g}}{\text{cm}^3}]$$

# DOSE EQUIVALENT

- Stopping power  $\approx$  LET,  $L \equiv dE/dx$ 
  - Units [ keV/ $\mu$ m ]
- Dose at a point becomes

$$D(x) = \sum_j \int_0^\infty dE L_j(E) \phi_j(x, E)$$

## DOSE EQUIVALENT

CALCULATED WITH DIFFERENTIAL FLUENCE  $\phi$

$$H(x) \equiv \sum_j \int_0^\infty dE Q(L_j) L_j(E) \phi_j(x, E) \quad [\text{Sv}]$$

$Q(L_j)$  = quality factor, function of LET, which is function of  $E$

$$\Rightarrow Q(L_j) \equiv Q(L_j(E))$$

# DOSE EQUIVALENT

Previous equation gives  $dD/dE = L_j(E)\phi_j(x, E)$ , so that

$$H(x) = \sum_j \int_0^\infty dD Q(L_j)$$

Defining [ICRU93, p.5]

$$D_L \equiv \frac{dD}{dL}$$

with units of  $\text{m kg}^{-1}$ , gives

$$H(x) = \sum_j \int_0^\infty dL D_L Q(L_j)$$

Note that it is *incorrect* to write

$$H(x) \neq \sum_j \int_0^\infty dL D(L) Q(L_j)$$



# EFFECTIVE DOSE

- Different tissues have different radiosensitivity

## EFFECTIVE DOSE

$$E \equiv \sum_T w_T H_T \quad [\text{Sv}]$$

# SUMMARY

Cross Sections  $\sigma_i$  ,  $\sigma_{ij}$  **PHYSICS** (NUCFRG, QMSFRG)

Boltzmann **TRANSPORT** Eqn  $\Rightarrow$  FLUENCE  $\phi_i$  [ $\#/\text{cm}^2/\text{MeV}$ ] (HZETRN)

$$\left[ \frac{\partial}{\partial x} - \frac{\partial}{\partial E} S_i(E) + \sigma_i(E) \right] \phi_i(x, E) = \sum_j \int_E^\infty dE' \sigma_{ij}(E, E') \phi_j(x, E')$$

$$\text{Dose } D(x) = \sum_i \int_0^\infty dE S_i(E) \phi_i(x, E) \quad [\text{Gy} = \text{J/kg}]$$

$$\text{Dose Equivalent } H(x) = \sum_i \int_0^\infty dE Q(L_i(E)) L_i(E) \phi_i(x, E) \quad [\text{Sv}]$$

$$\text{Effective Dose } E = \sum_T w_T H_T \quad [\text{Sv}] \quad \Rightarrow \text{Risk}$$

**BIOLOGY**  $Q(L_i), w_T$

$$L_i \equiv \frac{dE}{dx} \approx S_i(E)$$

## Leptons spin = 1/2

Flavor	Mass GeV/c <sup>2</sup>	Electric charge
$\nu_L$ lightest neutrino*	$(0-0.13)\times 10^{-9}$	0
$e$ electron	0.000511	-1
$\nu_M$ middle neutrino*	$(0.009-0.13)\times 10^{-9}$	0
$\mu$ muon	0.106	-1
$\nu_H$ heaviest neutrino*	$(0.04-0.14)\times 10^{-9}$	0
$\tau$ tau	1.777	-1

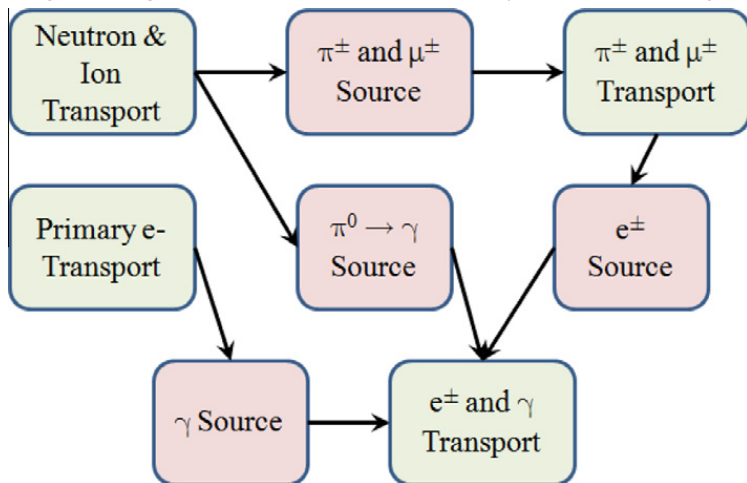
## Quarks spin = 1/2

Flavor	Approx. Mass GeV/c <sup>2</sup>	Electric charge
$u$ up	0.002	2/3
$d$ down	0.005	-1/3
$c$ charm	1.3	2/3
$s$ strange	0.1	-1/3
$t$ top	173	2/3
$b$ bottom	4.2	-1/3

Neutron, Proton = 3 quarks

Pion = 2 quarks

[Slaba, Blattinig, Reddell, Bahadori, Norman, Badavi, Advances Space Research 52, 62, 2013]



Flowchart of HZE- $\pi$ /EM transport model

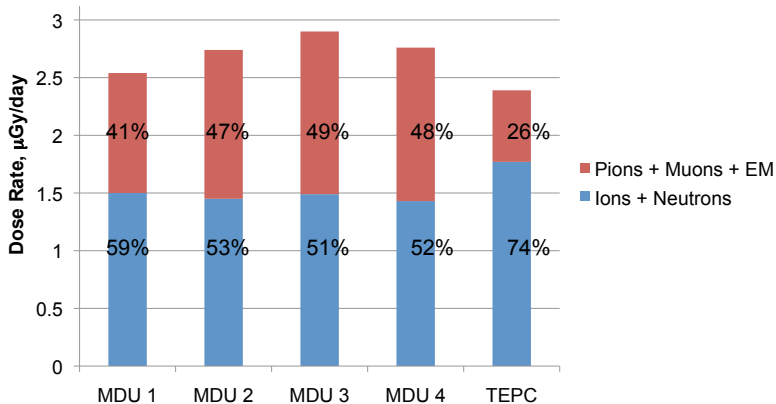
# PIONS MAKE LARGE CONTRIBUTIONS TO DOSE

[Slaba, Mertens, Blattnig, NASA TP-2013-217983]

[Norman, Blattnig, De Angelis, Badavi, Norbury: Advances Space Research 50, 146, 2012]

[Slaba, Blattnig, Reddell, Bahadori, Norman, Badavi: Advances Space Research 52, 62, 2013]

[Aghara, Blattnig, Norbury, Singleterry: Nucl. Inst. Meth. B 267, 1115, 2009]



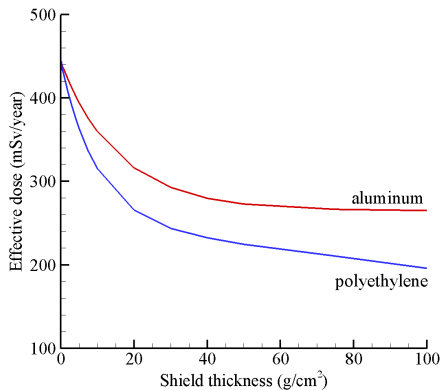
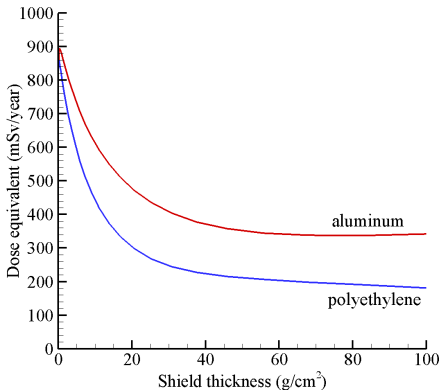
MDU=Mobile Dosimetry Unit (ISS)

## • Important discovery in space radiation

# MINIMUM IN DOSE EQUIVALENT VS. DEPTH

[Blattnig, Slaba, Bahadori, Norman, Cloudsley, Space Radiation Investigators' Workshop, Galveston, TX, 2014]

- Previous design paradigm
  - Exposures from GCR show little variation past 40 g/cm<sup>2</sup>
  - Increased shielding slightly decreases exposures
  - Transport performed with HZETRN (straight ahead transport with no pions)



BON2010 used to generate Oct 1976 GCR environment.

# MINIMUM IN DOSE EQUIVALENT VS. DEPTH

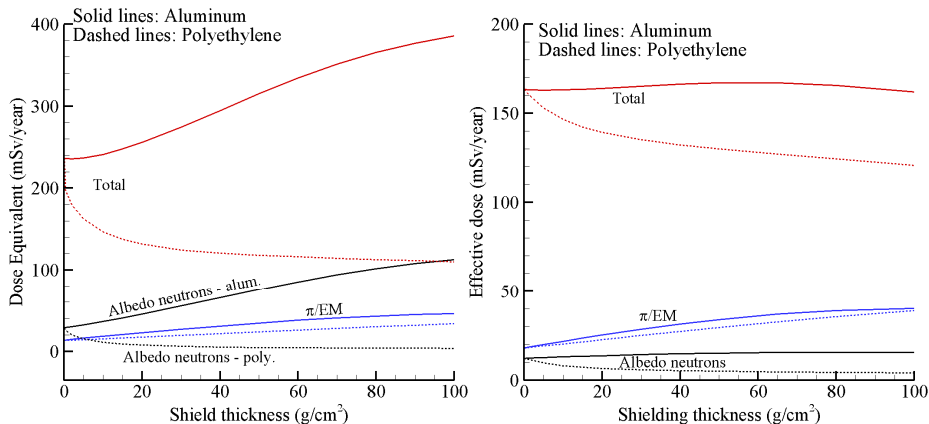


Figure 3. Dose equivalent (left pane) and effective dose (right pane) as a function of shield thickness on the Martian surface.

# MINIMUM IN DOSE EQUIVALENT VS. DEPTH

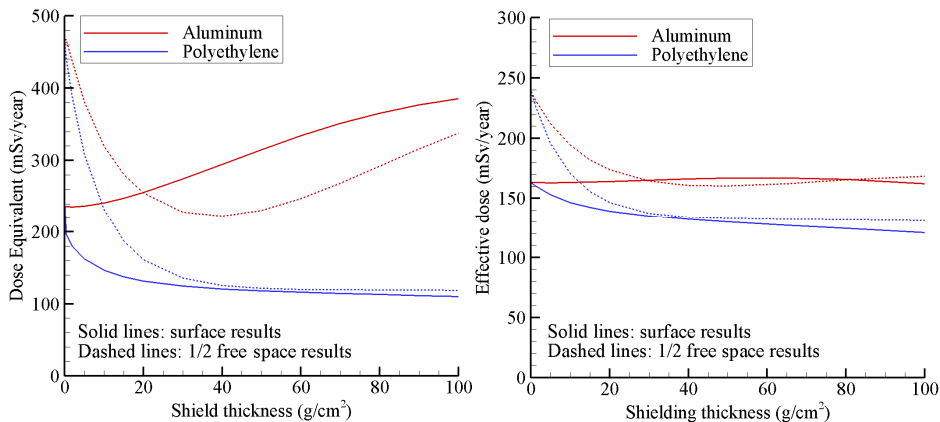


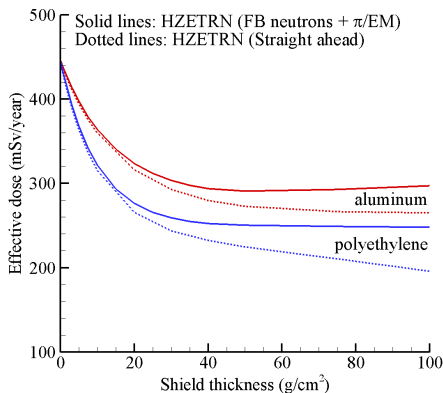
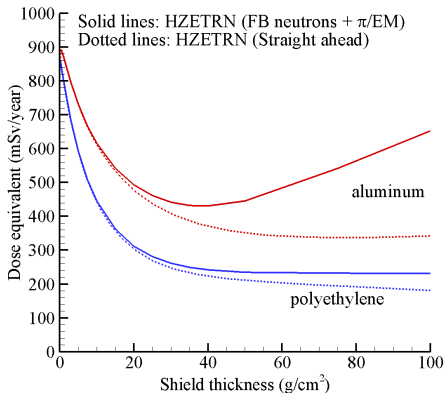
Figure 4. Comparison of surface exposure to  $\frac{1}{2}$  free space exposure as a function of shield thickness.



# MINIMUM IN DOSE EQUIVALENT VS. DEPTH

[Blattnig, Slaba, Bahadori, Norman, Cloudsley, Space Radiation Investigators' Workshop, Galveston, TX, 2014]

- New design paradigm
- If forward/backward (FB) neutron transport and pions turned ON
  - Minimum in dose equivalent vs. depth near 40 g/cm<sup>2</sup>
  - Increased shielding increases exposure
  - Material optimization more important than previously thought

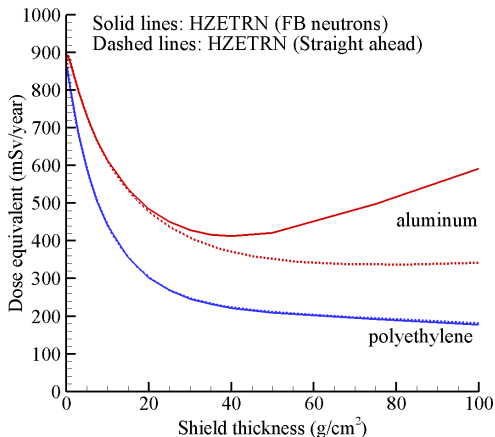
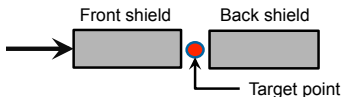


BON2010 used to generate Oct 1976 GCR environment.

# MINIMUM IN DOSE EQUIVALENT VS. DEPTH

[Blattnig, Slaba, Bahadori, Norman, Cloudsley, Space Radiation Investigators' Workshop, Galveston, TX, 2014]

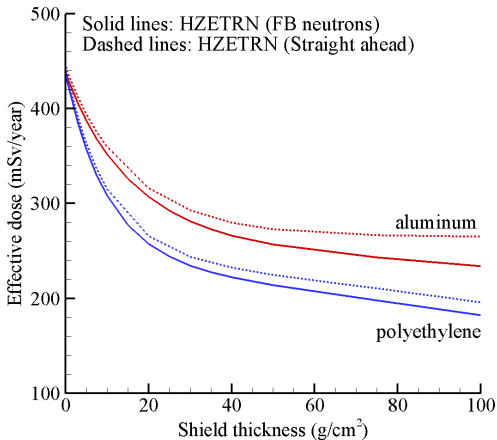
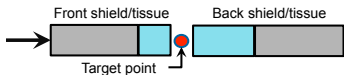
- Dose equiv in Al is result of neutron production & back-scatter in shielding behind target point
  - Back scattered neutrons produce high LET target fragments with short ranges



# MINIMUM IN DOSE EQUIVALENT VS. DEPTH

[Blattnig, Slaba, Bahadori, Norman, Cloudsley, Space Radiation Investigators' Workshop, Galveston, TX, 2014]

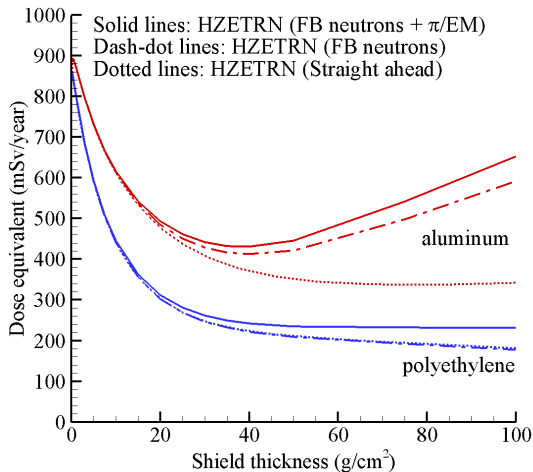
- Effective dose - body self shielding moderates neutron field & reduces impact of backward component
  - FB neutron transport accounts for multiple elastic collisions (moderation)



# MINIMUM IN DOSE EQUIVALENT VS. DEPTH

[Blattnig, Slaba, Bahadori, Norman, Cloudsley, Space Radiation Investigators' Workshop, Galveston, TX, 2014]

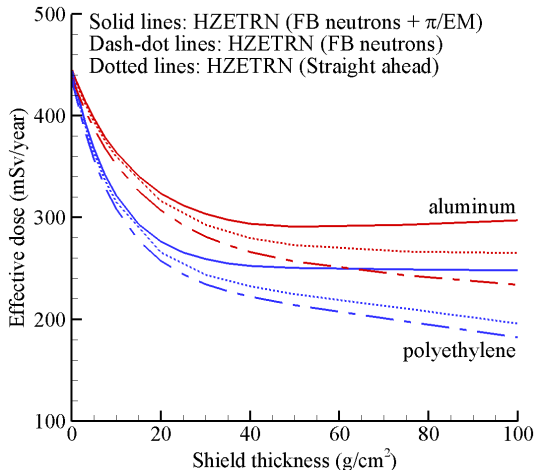
- Pion/EM contribution to dose equivalent smaller than contribution from neutrons, but still noticeable
  - Neutron contribution mainly from high LET target fragments (avg  $Q \sim 20$ )
  - Pion/EM avg  $Q \sim 1$



# MINIMUM IN DOSE EQUIVALENT VS. DEPTH

[Blattnig, Slaba, Bahadori, Norman, Cloudsley, Space Radiation Investigators' Workshop, Galveston, TX, 2014]

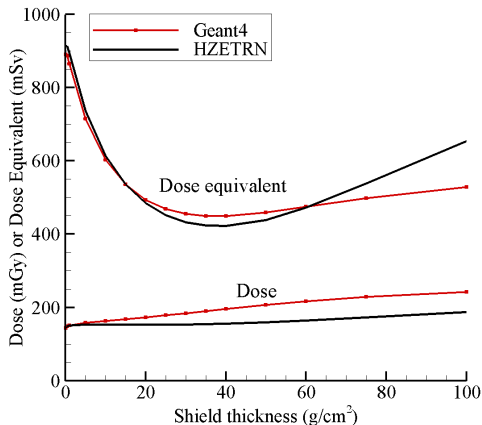
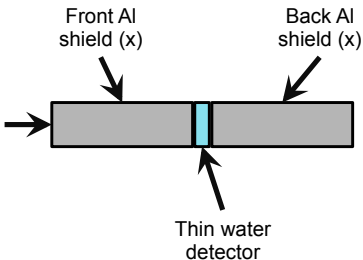
- Pion/EM contribution to effective dose more noticeable because tissue moderates/attenuates contribution from neutron field



# MINIMUM IN DOSE EQUIVALENT VS. DEPTH

[Blattnig, Slaba, Bahadori, Norman, Cloudsley, Space Radiation Investigators' Workshop, Galveston, TX, 2014]

- Verification
  - Preliminary comparison to Geant4



BON2010 used to generate solar minimum GCR environment ( $\phi = 475$  MV).

# MINIMUM IN DOSE EQUIVALENT VS. DEPTH

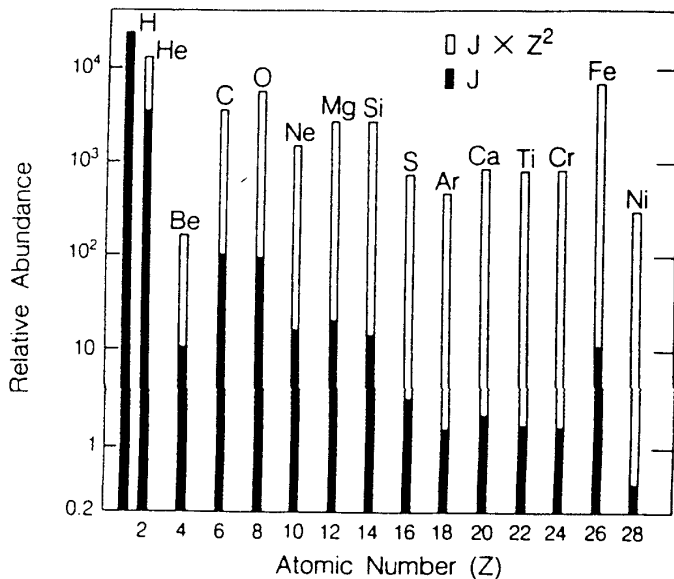
[Blattnig, Slaba, Bahadori, Norman, Cloudsley, Space Radiation Investigators' Workshop, Galveston, TX, 2014]

- Summary & Conclusions

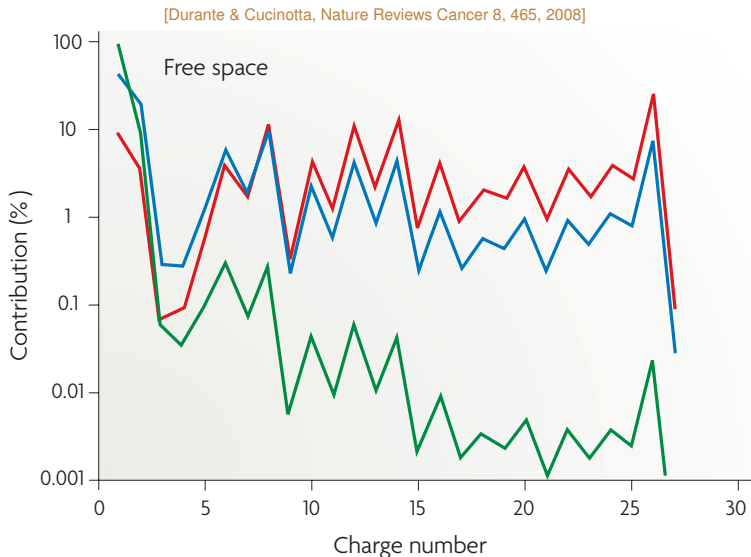
- New improvements to transport codes indicate potentially significantly different exposure vs. depth behavior in the region of 30-100 g/cm<sup>2</sup>
- Significant work has been done to confirm these findings but more is needed including:
  - More extensive benchmarking with Monte Carlo codes
  - Thick target experiments
- Vehicle and system designs may need to adapt to these new results including:
  - Renewed emphasis on materials optimization
  - Changes in configurations to avoid thicknesses where exposures are maximal

- NASA space radiation has focused on heavy ions (Fe)
  - Biology: majority of experiments at NSRL
  - Nuclear Physics: QMSFRG based on Eikonal approx
  - Transport: 1d HZETRN based on Straight-Ahead approx
- Reason →

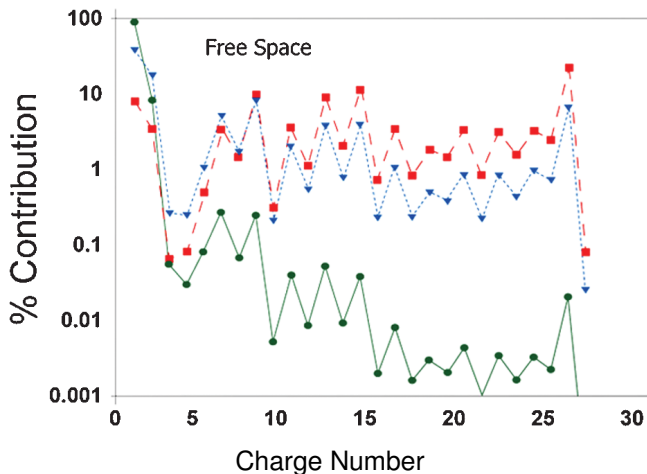




[NCRP Report No. 98]



GCR environment. Fluence, Dose, Dose equivalent.



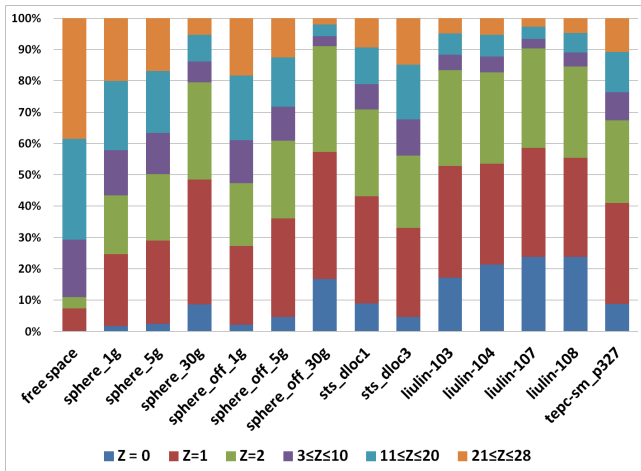
Relative contribution in **fluence**, **dose** and **dose equivalent** of different elements in the GCR spectrum. Calculation is an average over 1 year in solar minimum behind 5 g/cm<sup>2</sup> Al shielding.

[Durante & Cucinotta, Rev. Mod. Phys. 83, 1245, 2011]

BUT we don't have naked astronauts in free space . . .  
... and usually not thinly shielded

# INTERNAL ENVIRONMENT

[Walker, Townsend, Norbury, Advances in Space Research 51, 1792, 2013]



Percent contribution to **BFO** dose equivalent by charge group.

**Light ions & neutrons dominate!**

- NASA space radiation has focused on heavy ions (Fe)
  - OK for naked astronaut or thin shielding
  - Biology: more neutron, light ion experiments at NSRL
  - Not saying Heavy ions not important: need both heavy + light
- Neutrons & Light ions deflected at large angles
  - Nuclear Physics: QMSFRG based on Eikonal approx
  - Transport: 1d HZETRN based on Straight-Ahead approx
  - Both not adequate for neutrons, light ions
- Langley: 3d nuclear physics & 3d transport for neutrons, light ions
- Neutrons large Q, light ions highly penetrating
  - Accurate description → lower risk

- Heavy Ions in external environment
  - Produce the light ions and neutrons in the internal environment

# GCR SENSITIVITY ANALYSIS

- ACE = Advanced Composition Explorer
  - Earth-Sun L1 (1.5 million km from Earth)
  - CRIS Cosmic Ray Isotope Spectrometer
- AMS = Alpha Magnetic Spectrometer (on board ISS)
  - Search for dark matter, antimatter etc.
  - Also cosmic rays
- NSRL = NASA Space Radiation Lab
  - Brookhaven National Lab on Long Island
  - p - Fe    50 MeV/n - 1 GeV/n
  - up to Au    165 MeV/n
- FAIR = Facility for Antiproton and Ion Research
  - GSI Gesellschaft für Schwerionenforschung (Darmstadt)
  - Ne 45 GeV/n, U 35 GeV/n



# GCR SENSITIVITY ANALYSIS - 20 g/cm<sup>2</sup>

[Slaba & Blattnig, Space Weather, in press, 2014]

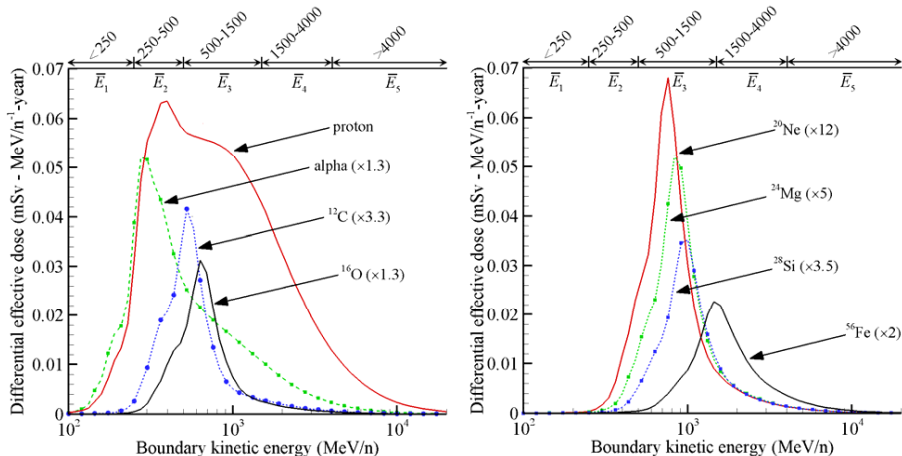


Figure 2. Differential effective dose rate as a function of boundary kinetic energy behind 20 g/cm<sup>2</sup> of aluminum exposed to solar minimum conditions described by BON2010 model. Results for specific ions have been scaled to improve plot clarity. The location of the peak distribution values along the horizontal axis indicates which boundary energies are most important to effective dose behind shielding.

GCR spectrum 90% effective dose > 500 MeV/n (ACE not helpful)

# GCR SENSITIVITY ANALYSIS - 0 g/cm<sup>2</sup>

Energy	Range	Satellite	Accelerator
$E_1$	$< 250 \text{ MeV}/n$	ACE, AMS	NSRL
$E_2$	$250 - 500 \text{ MeV}/n$	ACE, AMS	NSRL
$E_3$	$500 - 1500 \text{ MeV}/n$	AMS	NSRL, FAIR
$E_4$	$1500 - 4000 \text{ MeV}/n$	AMS	FAIR
$E_5$	$> 4000 \text{ MeV}/n$	AMS	FAIR

[Slaba & Blattnig, Space Weather, in press, 2014]

Table 1. Relative contribution ( $\times 100$ ) of GCR boundary energy and charge groups to effective dose with no shielding. A value of 0.0 indicates that the relative contribution is less than 0.1%. The BON2010 GCR model was used for these results during solar minimum conditions.

	$\bar{E}_1$	$\bar{E}_2$	$\bar{E}_3$	$\bar{E}_4$	$\bar{E}_5$	Total
Z = 1	2.1	3.7	11.6	10.5	7.7	35.6
Z = 2	2.1	1.4	2.5	1.6	0.9	8.4
Z = 3-10	4.1	5.5	2.6	1.0	0.6	13.8
Z = 11-20	1.4	6.0	7.7	2.7	1.5	19.3
Z = 21-28	0.4	3.0	11.1	5.5	3.0	22.9
Totals	10.0	19.5	35.6	21.3	13.6	100.0

$$E_3 + E_4 + E_5 = 70\%$$

$$E_4 + E_5 = 35\%$$

# GCR SENSITIVITY ANALYSIS - 20 g/cm<sup>2</sup>

Energy	Range	Satellite	Accelerator
$E_1$	$< 250 \text{ MeV}/n$	ACE, AMS	NSRL
$E_2$	$250 - 500 \text{ MeV}/n$	ACE, AMS	NSRL
$E_3$	$500 - 1500 \text{ MeV}/n$	AMS	NSRL, FAIR
$E_4$	$1500 - 4000 \text{ MeV}/n$	AMS	FAIR
$E_5$	$> 4000 \text{ MeV}/n$	AMS	FAIR

[Slaba & Blattnig, Space Weather, in press, 2014]

Table 2. Relative contribution ( $\times 100$ ) of GCR boundary energy and charge groups to effective dose with 20 g/cm<sup>2</sup> aluminum shielding. A value of 0.0 indicates that the relative contribution is less than 0.1%. The BON2010 GCR model was used for these results during solar minimum conditions.

	$\bar{E}_1$	$\bar{E}_2$	$\bar{E}_3$	$\bar{E}_4$	$\bar{E}_5$	Total
$Z = 1$	1.2	5.4	18.2	18.4	14.8	58.1
$Z = 2$	1.2	2.2	4.1	2.9	1.7	12.2
$Z = 3-10$	0.0	3.3	3.8	1.3	0.8	9.1
$Z = 11-20$	0.0	0.2	6.6	2.0	1.1	10.0
$Z = 21-28$	0.0	0.0	4.7	3.8	2.1	10.6
Totals	2.5	11.1	37.4	28.4	20.5	100.0

$$E_3 + E_4 + E_5 = 86\% \quad E_4 + E_5 = 49\%$$

# GCR SENSITIVITY ANALYSIS - 40 g/cm<sup>2</sup>

Energy	Range	Satellite	Accelerator
$E_1$	$< 250 \text{ MeV}/n$	ACE, AMS	NSRL
$E_2$	$250 - 500 \text{ MeV}/n$	ACE, AMS	NSRL
$E_3$	$500 - 1500 \text{ MeV}/n$	AMS	NSRL, FAIR
$E_4$	$1500 - 4000 \text{ MeV}/n$	AMS	FAIR
$E_5$	$> 4000 \text{ MeV}/n$	AMS	FAIR

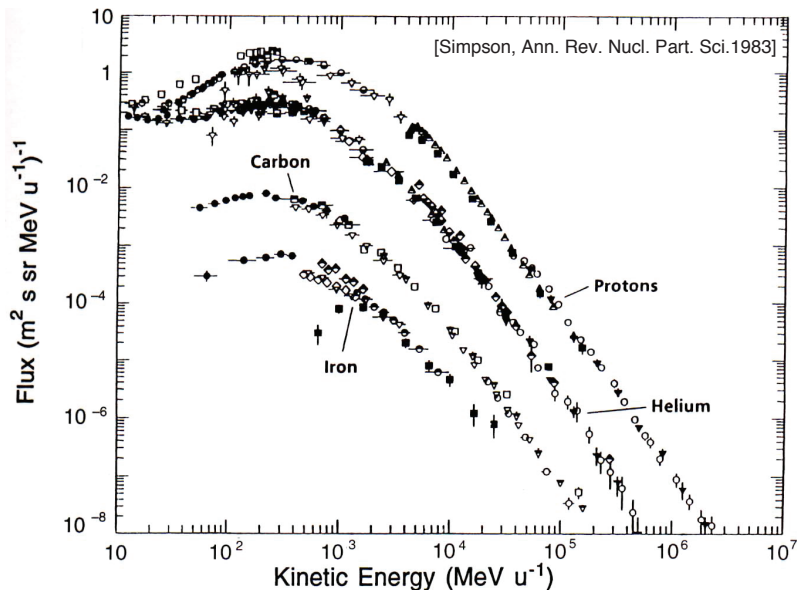
[Slaba & Blattnig, Space Weather, in press, 2014]

Table 3. Relative contribution ( $\times 100$ ) of GCR boundary energy and charge groups to effective dose with 40 g/cm<sup>2</sup> aluminum shielding. A value of 0.0 indicates that the relative contribution is less than 0.1%. The BON2010 GCR model was used for these results during solar minimum conditions.

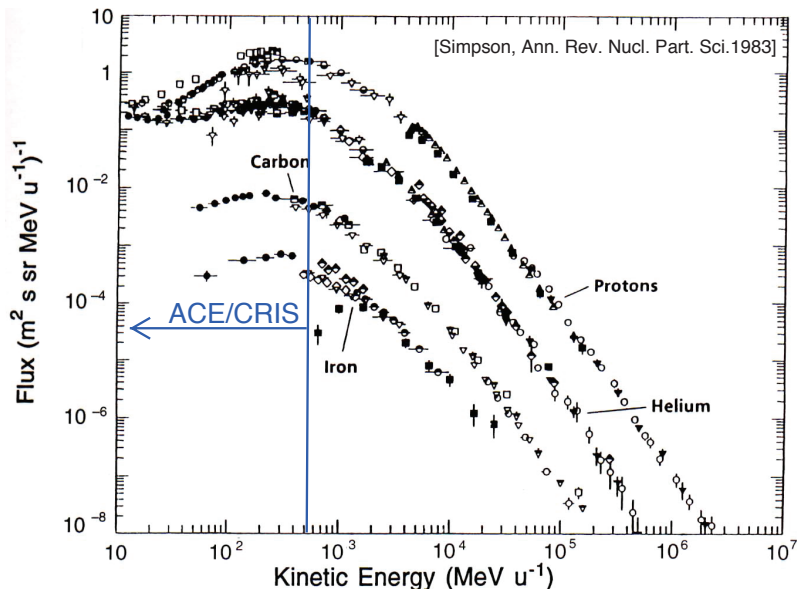
	$\bar{E}_1$	$\bar{E}_2$	$\bar{E}_3$	$\bar{E}_4$	$\bar{E}_5$	Total
$Z = 1$	0.2	5.4	20.9	23.0	20.0	69.6
$Z = 2$	0.1	2.5	4.9	3.9	2.5	14.0
$Z = 3-10$	0.0	0.5	3.9	1.4	0.9	6.7
$Z = 11-20$	0.0	0.0	2.9	1.4	0.8	5.1
$Z = 21-28$	0.0	0.0	1.1	2.3	1.2	4.6
Totals	0.3	8.5	33.8	32.0	25.4	100.0

$$E_3 + E_4 + E_5 = 91\% \quad E_4 + E_5 = 57\%$$

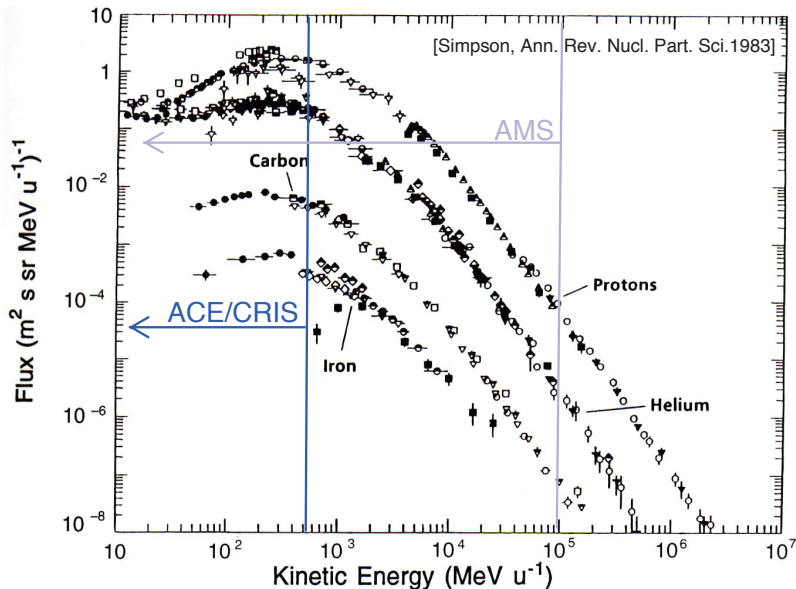
# GCR SENSITIVITY ANALYSIS



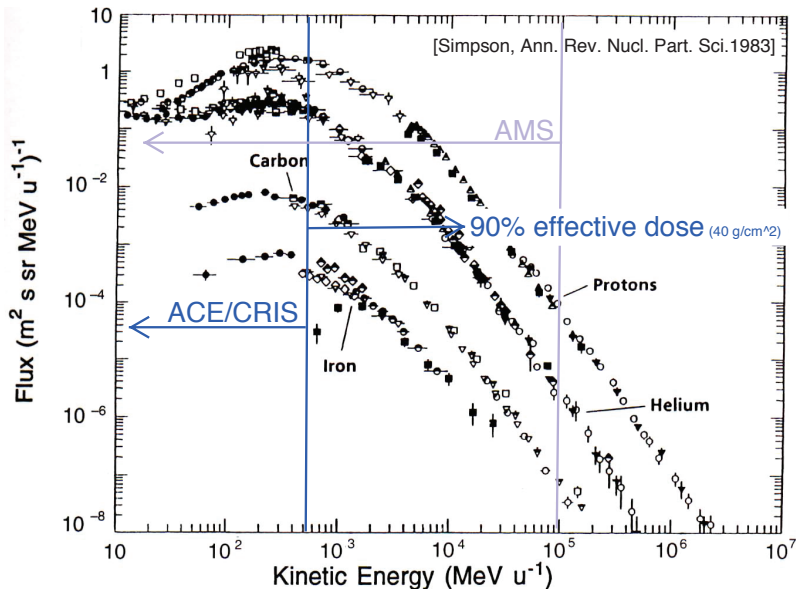
# GCR SENSITIVITY ANALYSIS



# GCR SENSITIVITY ANALYSIS

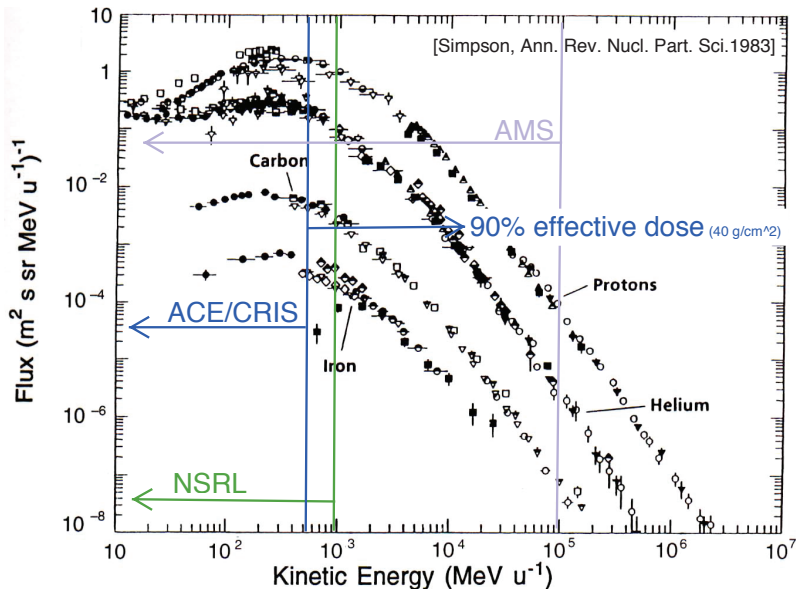


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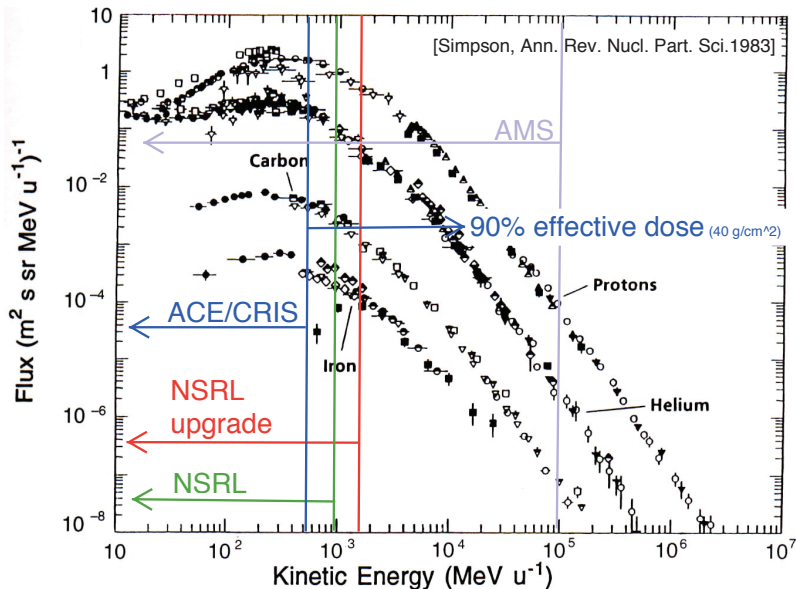




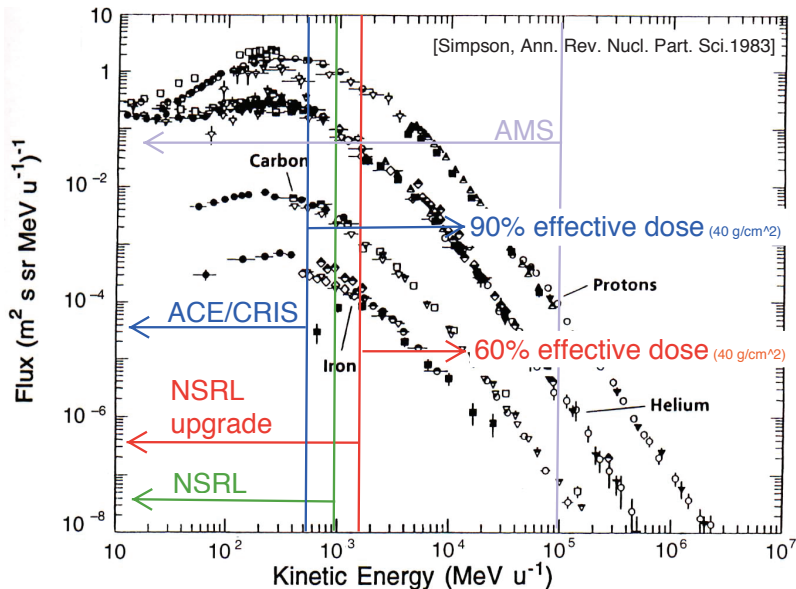
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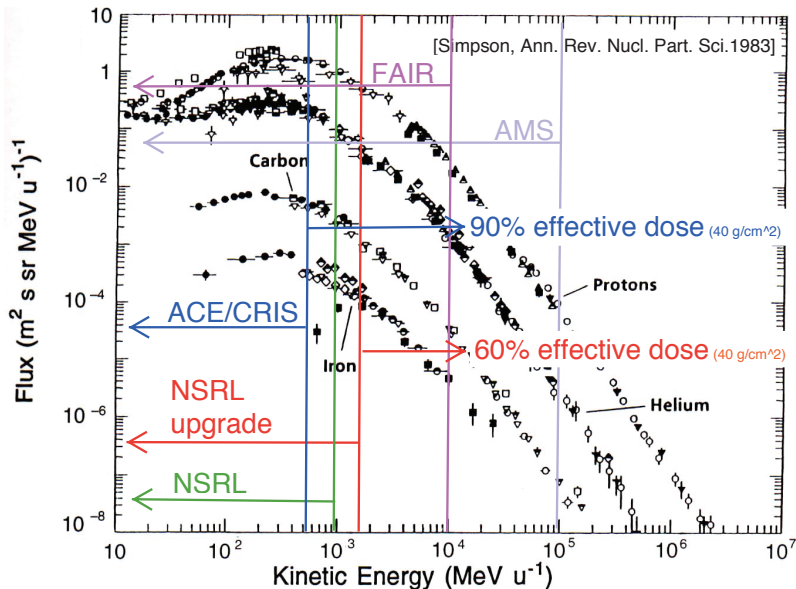
# GCR SENSITIVITY ANALYSIS



# GCR SENSITIVITY ANALYSIS



# GCR SENSITIVITY ANALYSIS



- No shielding (naked astronaut)

Satellites: ACE helpful, AMS much better

Accelerators: NSRL very useful, FAIR very useful

- Moderate shielding ( $20 \text{ g/cm}^2$ )

Satellites: ACE inadequate, AMS very useful

Accelerators: NSRL useful for low Z, FAIR useful for high Z

- Thicker shielding ( $40 \text{ g/cm}^2$ )

Satellites: ACE useless, AMS very useful

Accelerators: NSRL inadequate, FAIR very useful

## NASA Space Radiation Lab (NSRL):

- Wrong Ions (Z)?
  - Internal spectrum neutrons & light ions
- Wrong Flux (dose rate)?
  - Hormesis, Bystander, Fractionation, Countermeasures
- Wrong Energy (E)?
  - 60% effective dose  $> 1.5 \text{ GeV/n}$  (40 g/cm<sup>2</sup>)

# SUMMARY

- $E = 1 \text{ GeV/n}$ , really means  $T = 1 \text{ GeV/n}$
- Cross Section
  - Total, Differential, Angular, Spectral, Double Differential
- Transport
  - Flux, Fluence, Dose, Dose Equivalent
- Pions make significant contributions to dose
- Possible minimum in Dose equivalent vs. Depth curve
- ACE not sufficient - AMS needed
- NSRL not sufficient - FAIR needed

# THE END

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